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## 5-2 Study Guide and Intervention Solving Inequalities by Multiplication and Division

Solve Inequalities by Multiplication If each side of an inequality is multiplied by the same positive number, the resulting inequality is also true. However, if each side of an inequality is multiplied by the same negative number, the direction of the inequality must be reversed for the resulting inequality to be true.

| Multiplication Property of Inequalities | For all numbers $a, b$, and $c$, with $c \neq 0$, <br> 1. if $c$ is positive and $a>b$, then $a c>b c ;$ <br> if $c$ is positive and $a<b$, then $a c<b c ;$ <br> 2. if $c$ is negative and $a>b$, then $a c<b c ;$ <br> if $c$ is negative and $a<b$, then $a c>b c$. |
| :--- | :--- |

The property is also true when > and < are replaced with $\geq$ and $\leq$.

Example 1: Solve $-\frac{y}{8} \geq 12$

$$
\begin{array}{clll}
-\frac{y}{8} & \geq 12 & \text { Original inequality } & \frac{3}{4} k<15 \\
(-8)\left(-\frac{y}{8}\right) \leq(-8) 12 & & \text { Oultiply each side by }-8 \text {;change } \geq \text { to } \leq . & \left(\frac{4}{3}\right) \frac{3}{4} k<\left(\frac{4}{3}\right) 15 \\
y \leq-96 & \text { Simplify. } & \text { Multiply each side by } \frac{4}{3} . \\
k<20 & \text { Simplify. }
\end{array}
$$

The solution is $\{y \mid y \leq-96\}$.

Example 2: Solve $\frac{3}{4} k<15$

The solution is $\{k \mid k<20\}$.

## Exercises

Solve each inequality. Check your solution.

1. $\frac{y}{6} \leq 2$
2. $-\frac{n}{50}>22$
3. $\frac{3}{5} h \geq-3$
$\{y \mid y \leq 12\}$
$\{n \mid n<-1100\}$
$\{h \mid h \geq-5\}$
4. $-\frac{p}{6}<-6$
$\{p \mid p>36\}$
5. $\frac{1}{4} n \geq 10$
6. $-\frac{2}{3} b<\frac{1}{3}$
$\{n \mid n \geq 40\}$
$\left\{b \left\lvert\, b>-\frac{1}{2}\right.\right\}$
7. $\frac{3 m}{5}<-\frac{3}{20}$
$\left\{m \left\lvert\, m<-\frac{1}{4}\right.\right\}$
8. $-2.51 \leq-\frac{2 h}{4}$
$\{h \mid h \leq 5.02\}$
9. $\frac{g}{5} \geq-2$
10. $-\frac{3}{4}>-\frac{9 p}{5}$
$\left\{p \left\lvert\, p>\frac{5}{12}\right.\right\}$
11. $\frac{n}{10} \geq 5.4$
12. $\frac{2 a}{7} \geq-6$
$\{n \mid n \geq 54\}$
$\{a \mid a \geq-21\}$

Define a variable, write an inequality, and solve each problem. Check your solution.
13-15. Sample answer: Let $n=$ the number.
13. Half of a number is at least 14. $\frac{1}{2} n \geq 14 ;\{n \mid n \geq 28\}$
14. The opposite of one-third a number is greater than 9 . $-\frac{1}{3} n>9 ;\{n \mid n<-27\}$
15. One fifth of a number is at most $30 . \frac{1}{5} n \leq 30 ;\{n \mid n \leq 150\}$
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## 5-2 Study Guide and Intervention (continued) Solving Inequalities by Multiplication and Division

Solve Inequalities by Division If each side of a true inequality is divided by the same positive number, the resulting inequality is also true. However, if each side of an inequality is divided by the same negative number, the direction of the inequality symbol must be reversed for the resulting inequality to be true.

| Division Property of Inequalities | For all numbers $a, b$, and $c$ with $c \neq 0$, |
| :--- | :--- |
| 1. if $c$ is positive and $a>b$, then $\frac{a}{c}>\frac{b}{c}$; if $c$ is positive and $a<b$, then $\frac{a}{c}<\frac{b}{c} ;$ |  |
| 2. if $c$ is negative and $a>b$, then $\frac{a}{c}<\frac{b}{c}$; if $c$ is negative and $a<b$, then $\frac{a}{c}>\frac{b}{c}$. |  |

The property is also true when $>$ and $<$ are replaced with $\geq$ and $\leq$.
Example : Solve $-12 y \geq 48$.

| $-12 y$ | $\geq 48$ |  | Original inequality |
| ---: | :--- | ---: | :--- |
| $\frac{-12 y}{-12}$ | $\leq \frac{48}{-12}$ |  | Divide each side by -12 and change $\geq$ to $\leq$. |
| $y$ | $\leq-4$ |  | Simplify. |

The solution is $\{y \mid y \leq-4\}$.

## Exercises

Solve each inequality. Check your solution.

1. $25 g \geq-100$
$\{g \mid g \geq-4\}$
2. $-2 x \geq 9$

$$
\left\{x \left\lvert\, x \leq-4 \frac{1}{2}\right.\right\}
$$

6. $18<-3 b$
$\{b \mid b<-6\}$
7. $30<-3 n$
$\{n \mid n<-10\}$
8. $-2 n \geq 6.2$
$\{n \mid n \leq-3.1\}$
9. $-3<\frac{p}{4}$
$\{p \mid p>-12\}$
10. $-5 c>2$

$$
\left\{c \left\lvert\, c<-\frac{2}{5}\right.\right\}
$$

4. $-8 m<-64$
$\{m \mid m>8\}$
5. $-6 k<\frac{1}{5}$
$\left\{k \left\lvert\, k>-\frac{1}{30}\right.\right\}$
6. $-30>-5 p$
$\{p \mid p>6\}$
7. $-\frac{2}{3} n \geq 6$
$\{n \mid n \leq-9\}$
8. $-0.24<0.6 w$
$\{w \mid w>-0.4\}$
9. $\begin{aligned} & 25 \geq-2 m \\ & \left\{m \left\lvert\, m \geq-12 \frac{1}{2}\right.\right\}\end{aligned}$
10. $-40>10 h$
$\{h \mid h<-4\}$

Define a variable, write an inequality, and solve each problem. Then check your solution.
17-19. Sample answer: Let $n=$ the number.
17. Four times a number is no more than 108. $4 n \leq 108 ;\{n \mid n \leq 27\}$
18. The opposite of three times a number is greater than 12. $-3 n>12 ;\{n \mid n<-4\}$
19. Negative five times a number is at most 100. $-5 n \leq 100 ;\{n \mid n \geq-20\}$

