

# 4-1 Study Guide and Intervention

## Writing Equations in Slope-Intercept Form

**Write an Equation Given the Slope and a Point** You can write an equation of a line if you are given a slope and a point other than the y-intercept.

**Example 1:** Write an equation of the line that passes through  $(-4, 2)$  with a slope of 3.

The line has slope 3. To find the y-intercept, replace  $m$  with 3 and  $(x, y)$  with  $(-4, 2)$  in the slope-intercept form. Then solve for  $b$ .

$$y = mx + b \quad \text{Slope-intercept form}$$

$$2 = 3(-4) + b \quad m = 3, y = 2, \text{ and } x = -4$$

$$2 = -12 + b \quad \text{Multiply.}$$

$$14 = b \quad \text{Add 12 to each side.}$$

Therefore, the equation is  $y = 3x + 14$ .

**Example 2:** Write an equation of the line that passes through  $(-2, -1)$  with a slope of  $\frac{1}{4}$ .

The line has slope  $\frac{1}{4}$ . Replace  $m$  with  $\frac{1}{4}$  and  $(x, y)$  with  $(-2, -1)$  in the slope-intercept form.

$$y = mx + b \quad \text{Slope-intercept form}$$

$$-1 = \frac{1}{4}(-2) + b \quad m = \frac{1}{4}, y = -1, \text{ and } x = -2$$

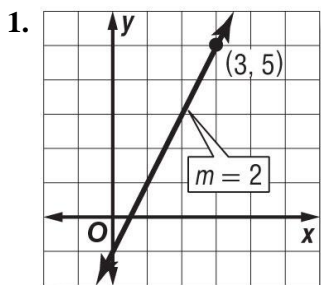
$$-1 = -\frac{1}{2} + b \quad \text{Multiply.}$$

$$-\frac{1}{2} = b \quad \text{Add } \frac{1}{2} \text{ to each side.}$$

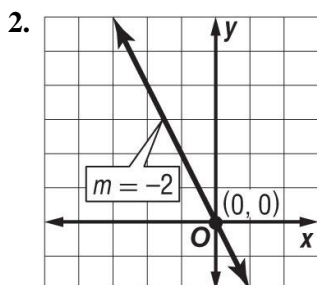
Therefore, the equation is  $y = \frac{1}{4}x - \frac{1}{2}$ .

### Exercises

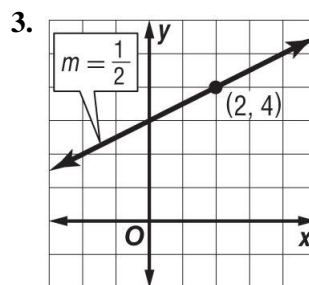
Write an equation of the line that passes through the given point and has the given slope.



$$y = 2x - 1$$



$$y = -2x$$



$$y = \frac{1}{2}x + 3$$

4.  $(8, 2)$ ; slope  $-\frac{3}{4}$   

$$y = -\frac{3}{4}x + 8$$

5.  $(-1, -3)$ ; slope 5  

$$y = 5x + 2$$

6.  $(4, -5)$ ; slope  $-\frac{1}{2}$   

$$y = -\frac{1}{2}x - 3$$

7.  $(-5, 4)$ ; slope 0  

$$y = 4$$

8.  $(2, 2)$ ; slope  $\frac{1}{2}$   

$$y = \frac{1}{2}x + 1$$

9.  $(1, -4)$ ; slope  $-6$   

$$y = -6x + 2$$

10.  $(-3, 0)$ ,  $m = 2$   

$$y = 2x + 6$$

11.  $(0, 4)$ ,  $m = -3$   

$$y = -3x + 4$$

12.  $(0, 350)$ ,  $m = \frac{1}{5}$   

$$y = \frac{1}{5}x + 350$$

# 4-1 Study Guide and Intervention (continued)

## Writing Equations in Slope-Intercept Form

**Write an Equation Given Two Points** If you are given two points through which a line passes, you can use them to find the slope first. Then you can use that slope and one of the points to write the equation of the line.

**Example: Write an equation of the line that passes through (1, 2) and (3, -2).**

Find the slope  $m$ . To find the  $y$ -intercept, replace  $m$  with its computed value and  $(x, y)$  with  $(1, 2)$  in the slope-intercept form. Then solve for  $b$ .

$$m = \frac{y_2 - y_1}{x_2 - x_1}$$

Slope formula

$$m = \frac{-2 - 2}{3 - 1}$$

$$y_2 = -2, y_1 = 2, x_2 = 3, x_1 = 1$$

$$m = -2$$

Simplify.

$$y = mx + b$$

Slope-intercept form

$$2 = -2(1) + b$$

Replace  $m$  with  $-2$ ,  $y$  with  $2$ , and  $x$  with  $1$ .

$$2 = -2 + b$$

Multiply.

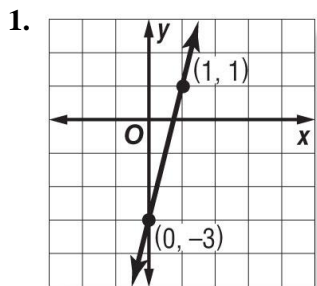
$$4 = b$$

Add 2 to each side.

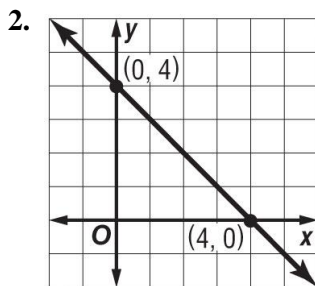
Therefore, the equation is  $y = -2x + 4$ .

### Exercises

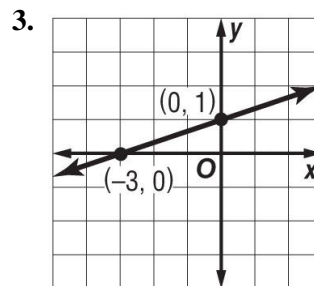
Write an equation of the line that passes through each pair of points.



$$y = 4x - 3$$



$$y = -x + 4$$



$$y = \frac{1}{3}x + 1$$

4.  $(-1, 6), (7, -10)$

$$y = -2x + 4$$

5.  $(0, 2), (1, 7)$

$$y = 5x + 2$$

6.  $(6, -25), (-1, 3)$

$$y = -4x - 1$$

7.  $(-2, -1), (2, 11)$

$$y = 3x + 5$$

8.  $(10, -1), (4, 2)$

$$y = -\frac{1}{2}x + 4$$

9.  $(-14, -2), (7, 7)$

$$y = \frac{3}{7}x + 4$$

10.  $(4, 0), (0, 2)$

$$y = -\frac{1}{2}x + 2$$

11.  $(-3, 0), (0, 5)$

$$y = \frac{5}{3}x + 5$$

12.  $(0, 16), (-10, 0)$

$$y = \frac{8}{5}x + 16$$